

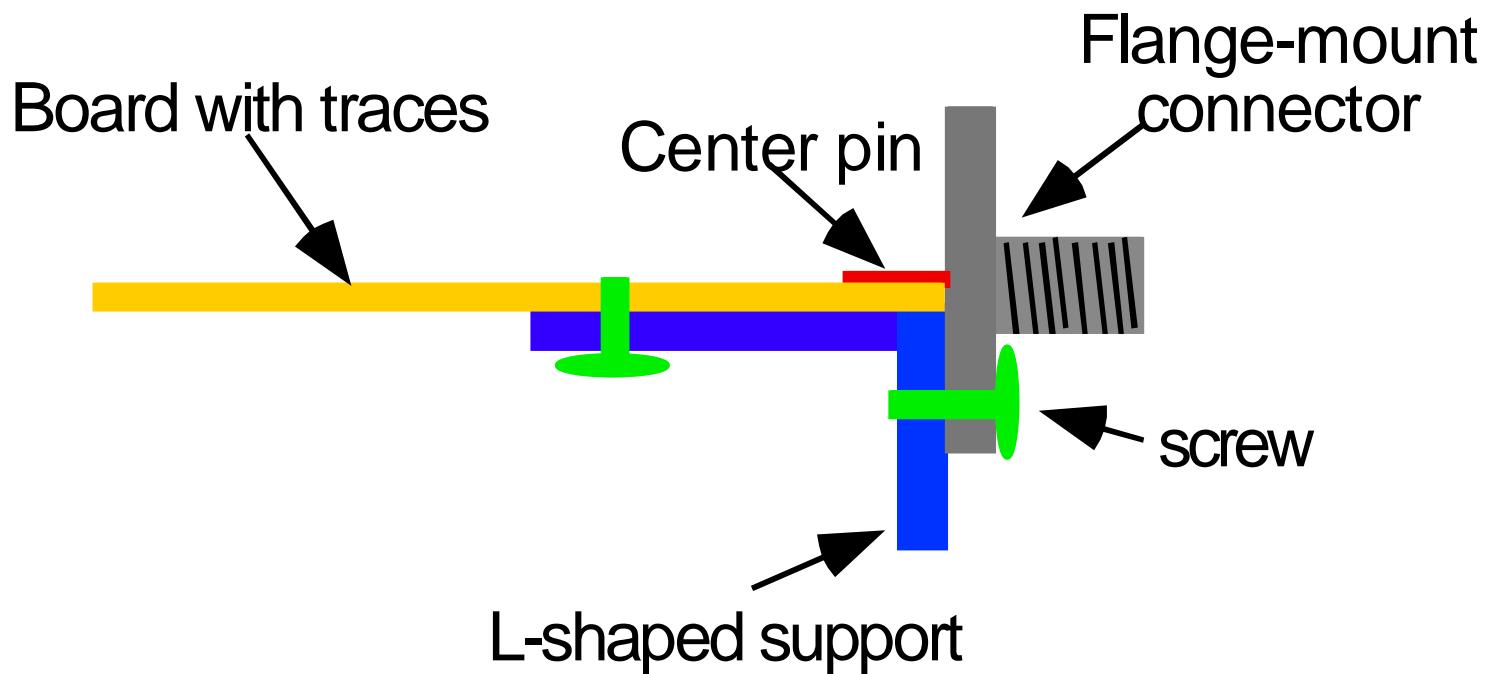
# ECE 451

## Automated Microwave Measurements

## TL Characterization

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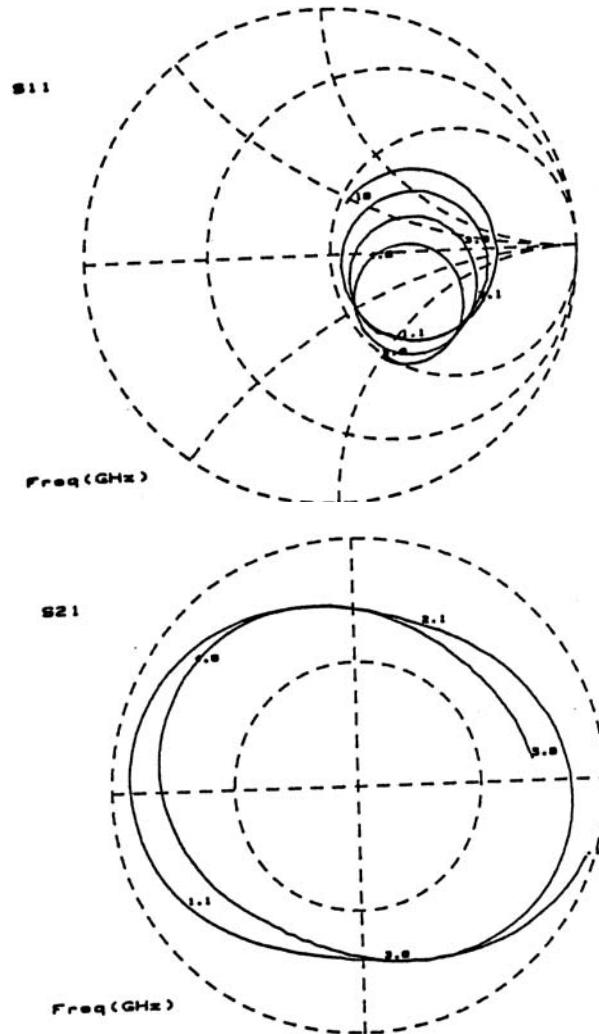
# Coaxial-Microstrip Transition



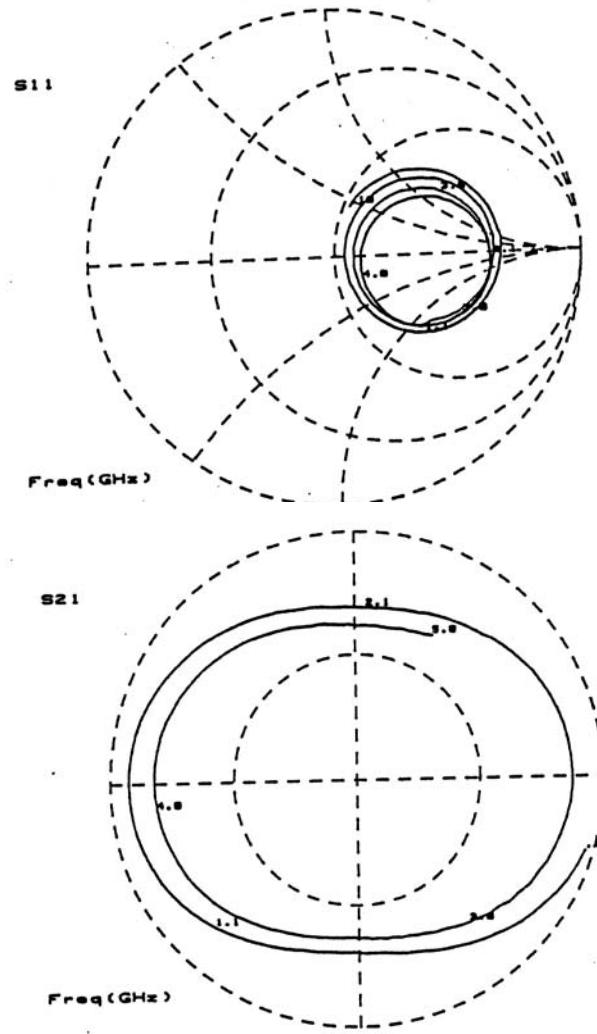
**Remove effects of discontinuities before processing data!**

# Coaxial-Microstrip Transition

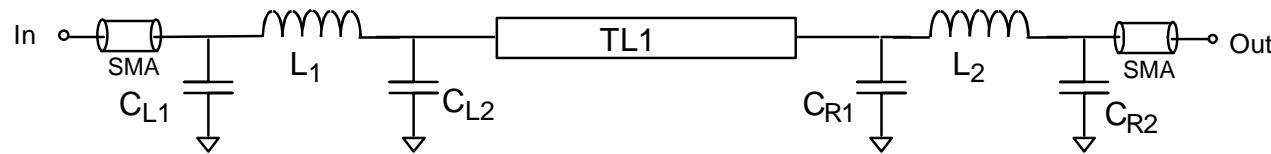
With parasitics



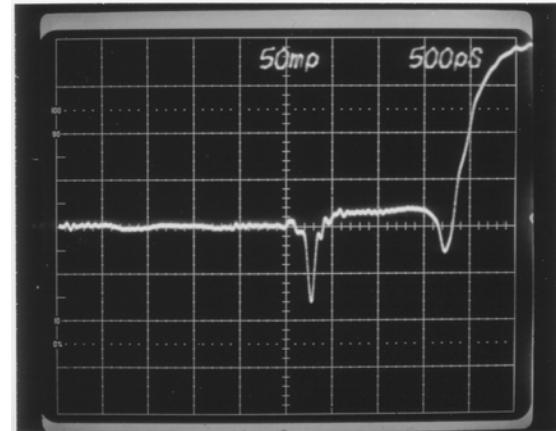
No parasitics



# Coaxial-Microstrip Transition

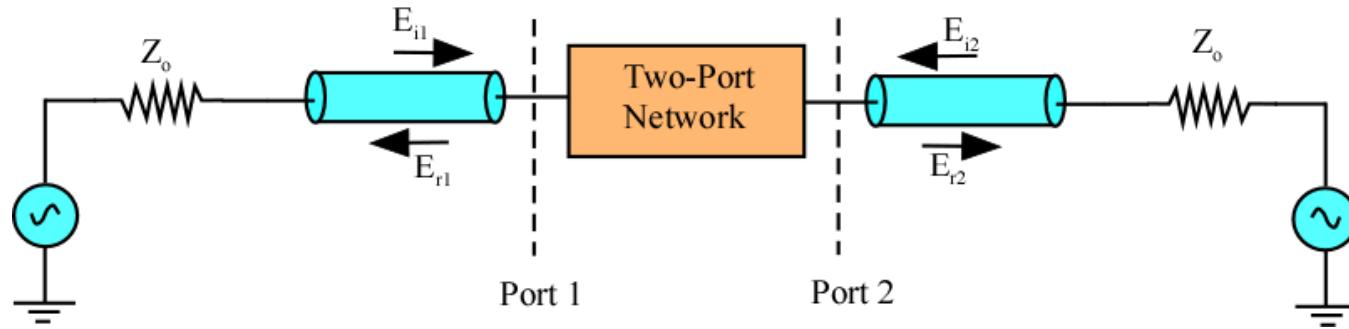


Equivalent Circuit



TDR Plot

# High-Frequency Characterization



## Transmission-Line Scattering Parameters

$$S_{21} = \frac{(1 - \Gamma^2)X}{1 - \Gamma^2 X^2} \quad S_{11} = \frac{(1 - X^2)\Gamma}{1 - \Gamma^2 X^2}$$

$$X = e^{-\gamma d}$$

$$Z_c = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

$$\Gamma = \frac{Z_c - Z_o}{Z_c + Z_o} \quad \gamma = \sqrt{(R + j\omega L)(G + j\omega C)}$$

# TL Extraction Formulas

$$X = e^{-\gamma d} = e^{-j\beta d} e^{-\alpha d} \quad X = e^{-\gamma d} = \frac{(S_{11} + S_{21}) - \Gamma}{1 - (S_{11} + S_{21})\Gamma}$$

$$\Gamma = Q \pm \sqrt{Q^2 - 1}$$

$$Q = \frac{\{S_{11}^2 - S_{21}^2\} + 1}{2S_{11}}$$

$$R = \text{Re}\{\gamma Z_c\}$$

$$G = \text{Re}\left\{\frac{\gamma}{Z_c}\right\}$$

$$L = \frac{1}{\omega} \text{Im}\{Z_c \gamma\}$$

$$C = \frac{1}{\omega} \text{Im}\left\{\frac{\gamma}{Z_c}\right\}$$

# Low-Loss Approximation

If we assume  $R \ll \omega L$

and  $G \ll \omega C$

$$Z_c \cong \sqrt{\frac{L}{C}}$$

$$\gamma \cong \frac{R}{2} \sqrt{\frac{C}{L}} + j\omega\sqrt{LC} = \frac{R}{2Z_c} + j\frac{\omega}{v_p}$$

$$\alpha \cong \frac{R}{2Z_c} \quad \beta \cong \frac{\omega}{v_p}$$

# TL Extraction Formulas

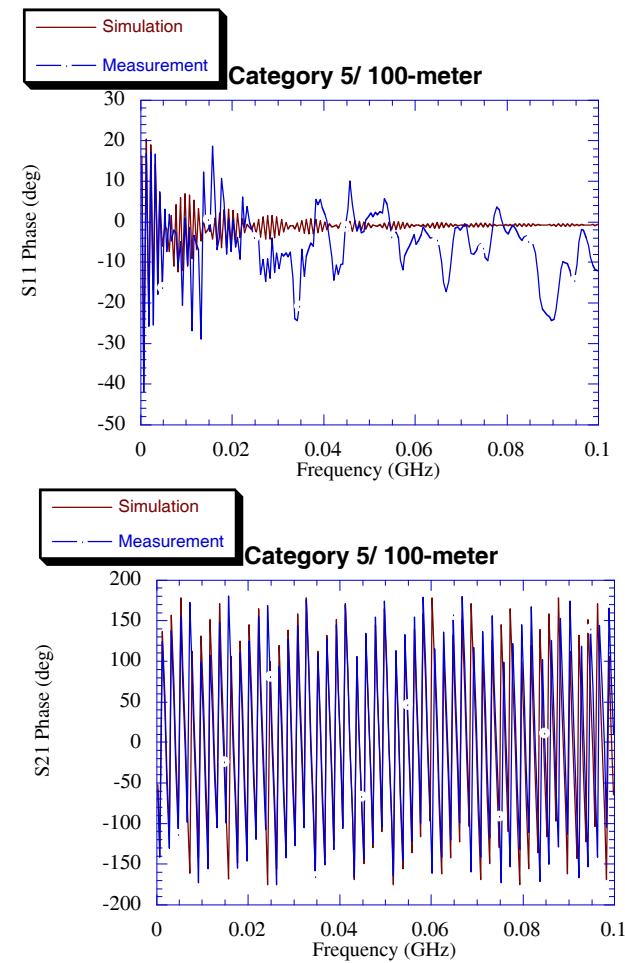
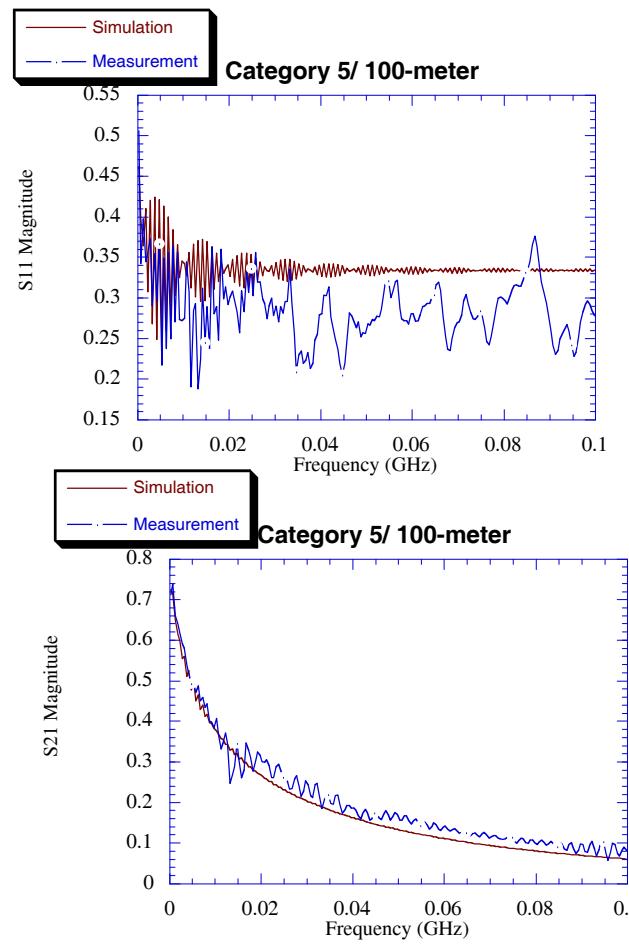
$$\alpha = -\frac{\ln(|X|)}{d}$$

$$R = -\frac{2Z_c \ln(|X|)}{d}$$

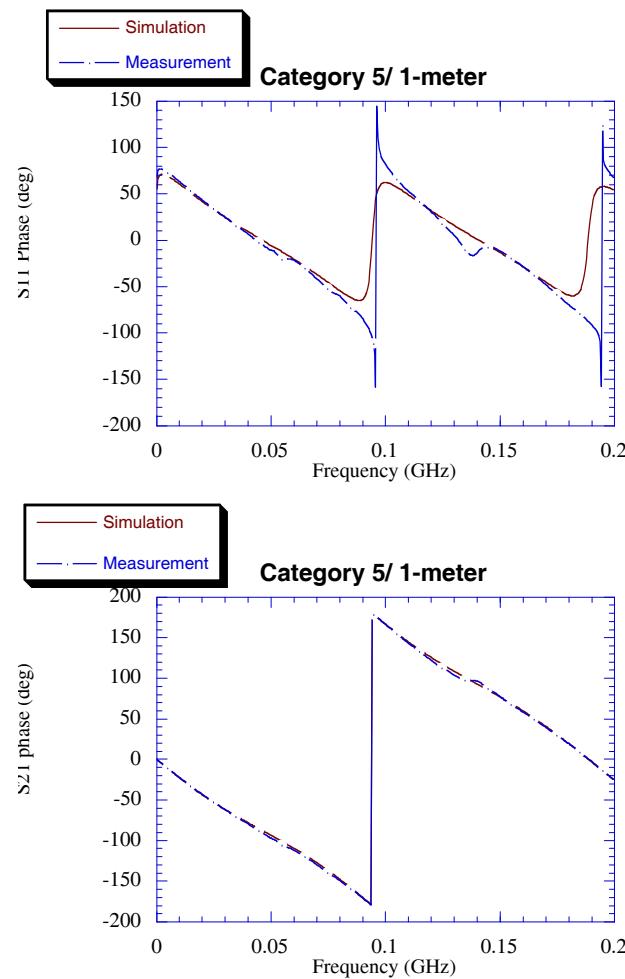
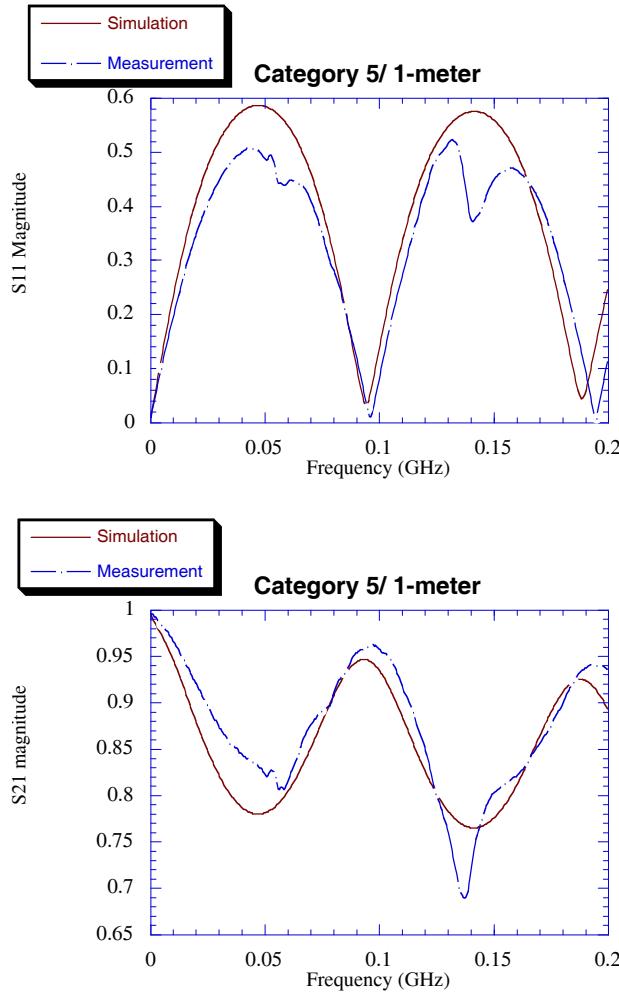
$$\frac{\Delta\phi}{\Delta\omega} = -\frac{d}{v_p}$$

$$v_p = -\frac{d}{\frac{\Delta\phi}{\Delta\omega}}$$

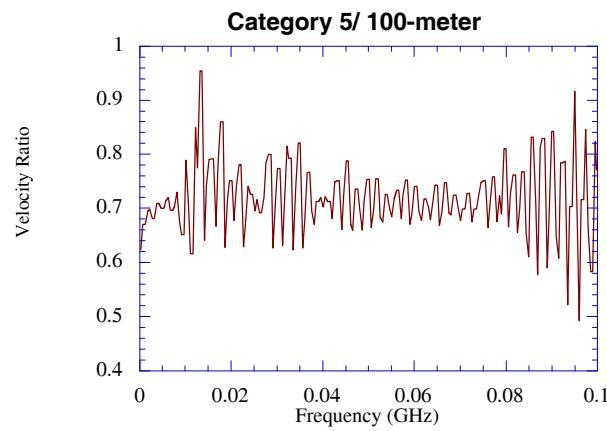
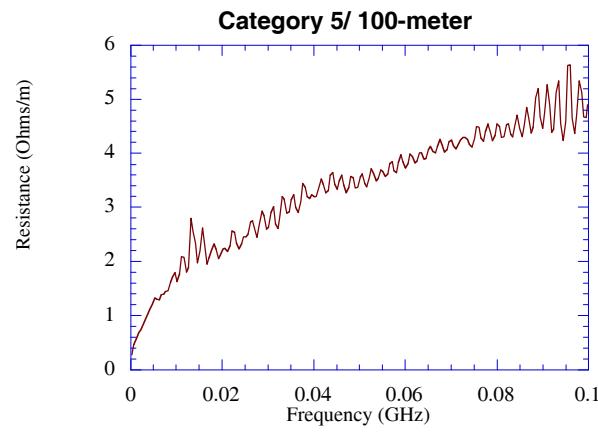
# Example: Category-5 Cable (long)



# Example: Category-5 Cable (short)



# Category-5 Cable – Loss Characteristics



# Cable Loss Model

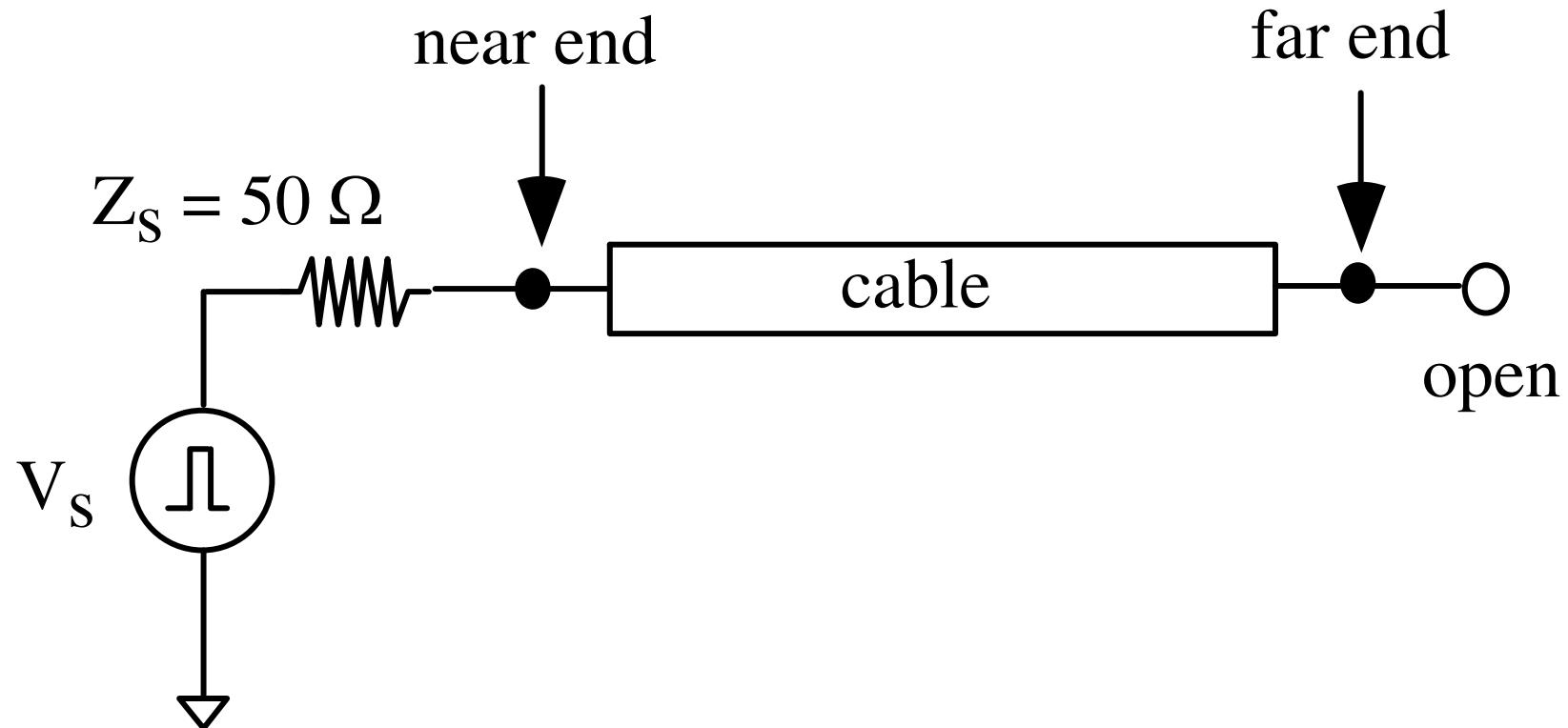
$$R(f) = R_s * f^p$$

$$\nu_r = \nu_{ro} + \nu_{rs} * f$$

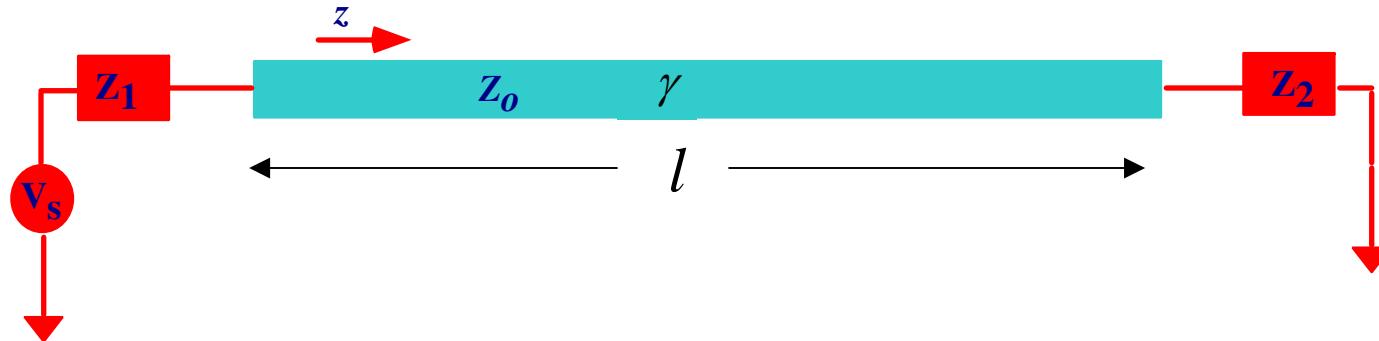
$$Z = R(f) + j\omega L = R_{skin} + j(R_{skin} + \omega L)$$

	$Z_0$ ( $\Omega$ )	$V_{ro}$ (m/ns)	$V_{rs}$ (m/ns-GHz)	$R_s$ ( $\Omega/m \cdot GHz^p$ )	$p$	$f_{max}$ (GHz)
<b>Category 5</b>	100	0.724	-0.165	15.38	0.482	0.2
<b>24-Ga</b>	100	0.678	1.157	29.03	0.593	0.1
<b>Category 3</b>	100	0.705	11.06	12.31	0.473	0.01
<b>SMA</b>	50	0.700	0.113	7.94	0.415	0.2

# Time-Domain Simulations



# Lossy Transmission Line

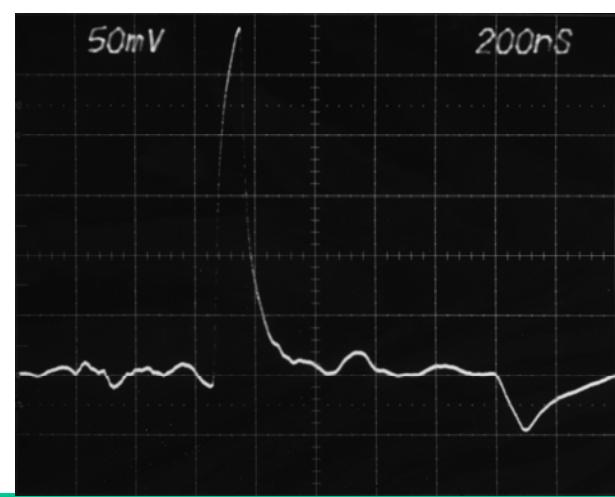
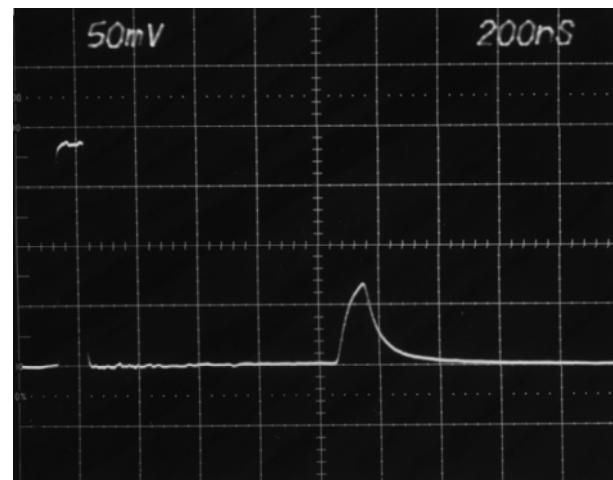
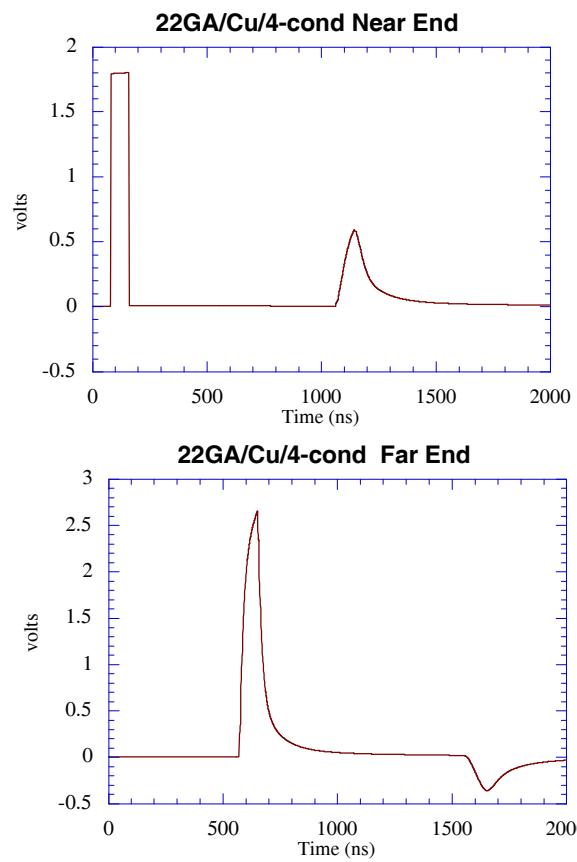


$$V(z) = A e^{-\alpha z} e^{-j\beta z} + B e^{+\alpha z} e^{+j\beta z}$$

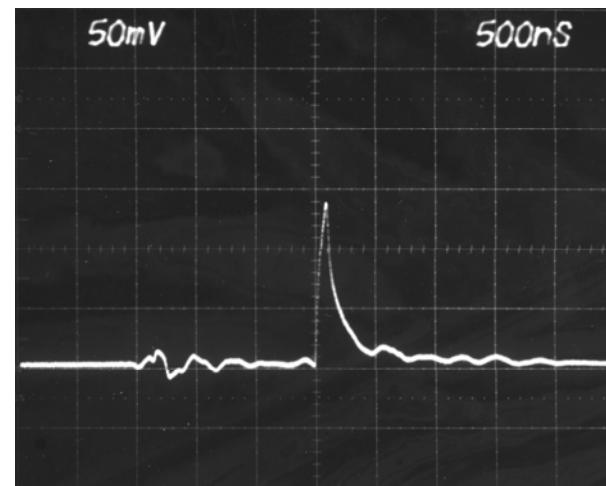
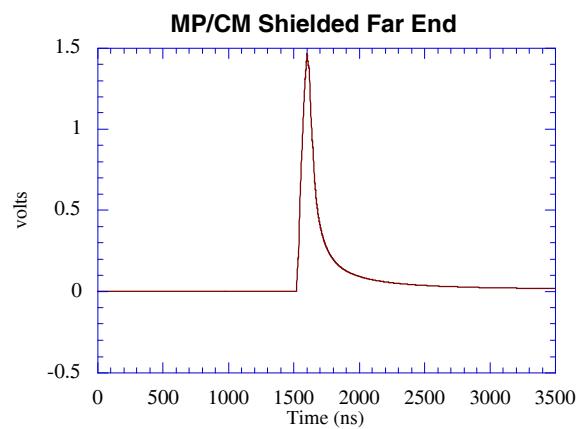
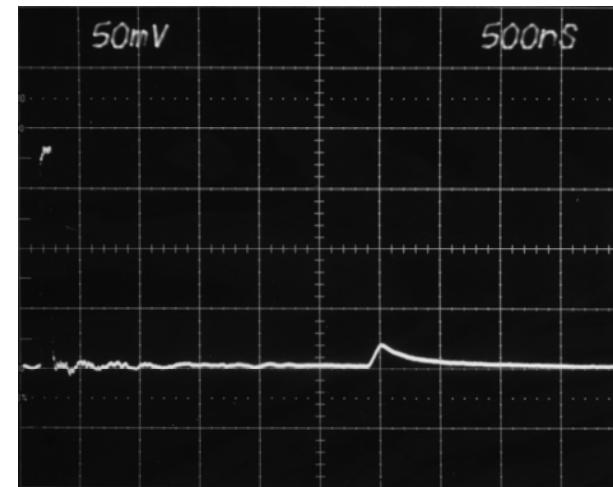
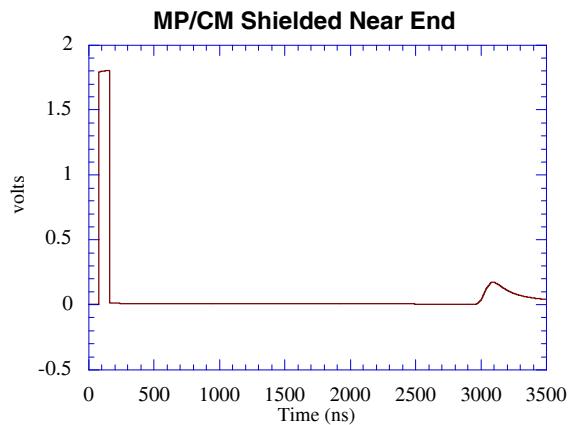
$$I(z) = \frac{1}{Z_o} [A e^{-\alpha z} e^{-j\beta z} - B e^{+\alpha z} e^{+j\beta z}]$$

$$Z_o = \sqrt{\frac{(R(\omega) + j\omega L)}{(G + j\omega C)}} \quad \gamma = \alpha + j\beta = \sqrt{(R(\omega) + j\omega L)(G + j\omega C)}$$

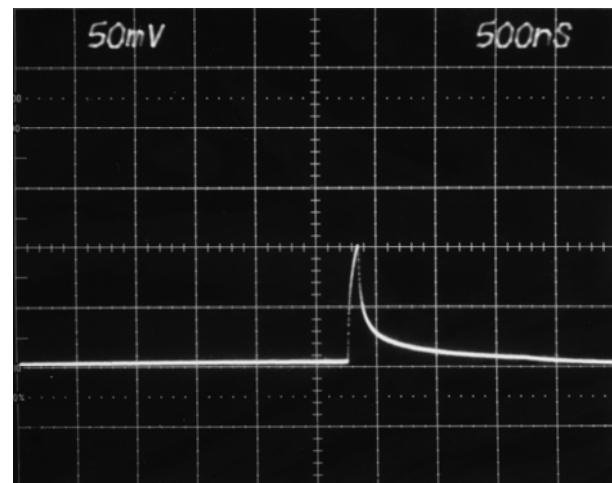
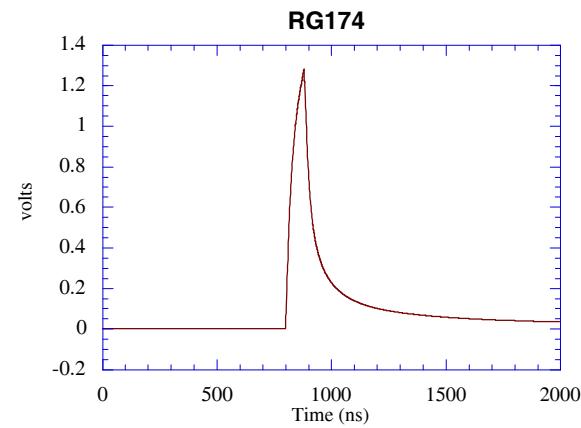
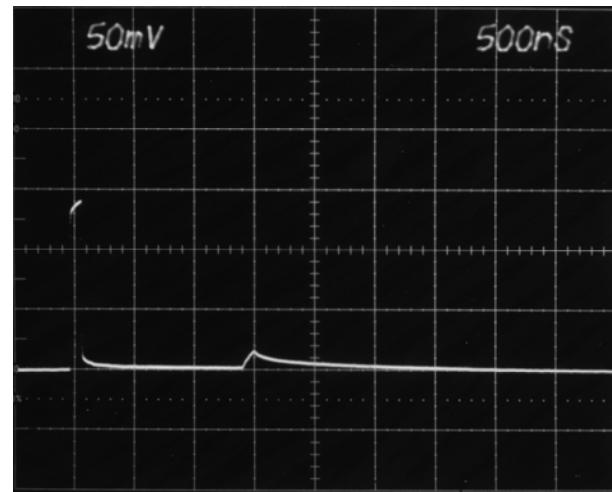
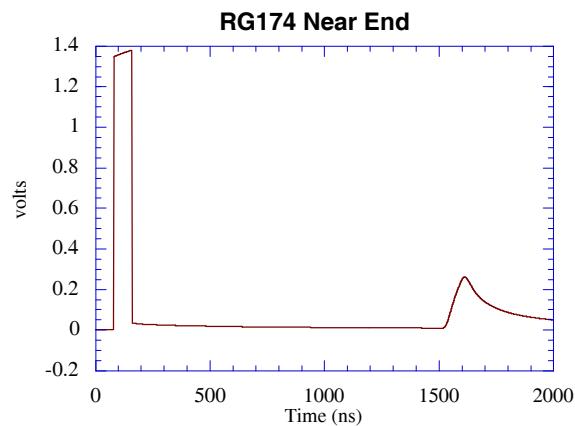
# Pulse Propagation (CAT-5)



# Pulse Propagation (MP/CM)

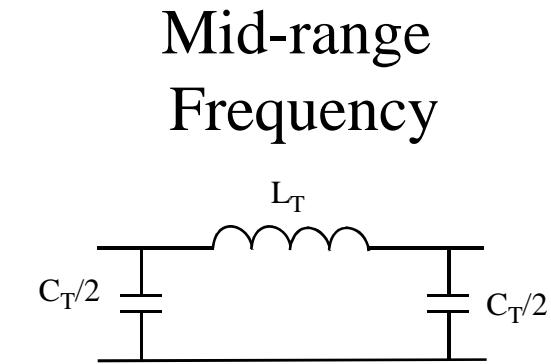


# Pulse Propagation (RG174)

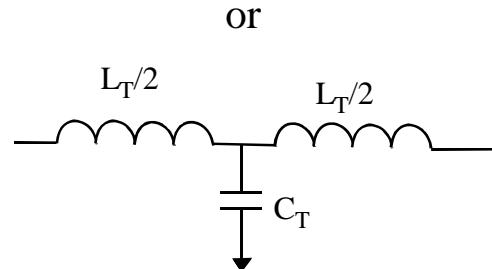


# Modeling Interconnections

Low Frequency

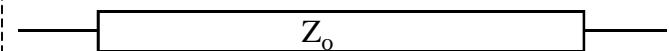


Short



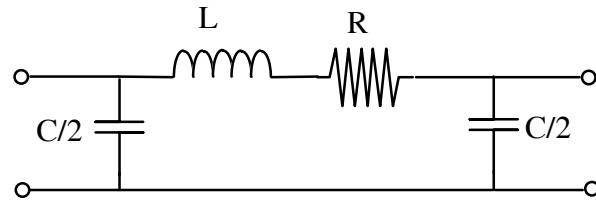
Lumped  
Reactive CKT

High Frequency



Transmission  
Line

# Low-Frequency TL Approximation



$$P = (R + j\omega L)(1 + j\omega CZ_o/2)$$

$$Y = j\omega CZ_o/2$$

$$S_{11} = \frac{P - 2YZ_o - YP}{2Z_o + P + 2YZ_o + YP} \quad S_{21} = \frac{2Z_o}{2Z_o + P + 2YZ_o + YP}$$

$$A = 2Z_o(1 - S_{21})$$

$$Y = \frac{A - 2S_{11}S_{21}Z_o - S_{11}A}{4S_{21}Z_o + 2S_{11}S_{21}Z_o + S_{11}A + A} \quad P = A - 2YS_{21}Z_oS_{21}(1 + Y)$$

# Low-Frequency Model for Microstrip

- Lumped Model
- Use extraction algorithm

