

1. A parallel-plate waveguide is filled with a dielectric $\epsilon = 9\epsilon_0$ and $\mu = \mu_0$. The separation between the plates is 2.5 cm. Determine the propagating modes for a wave of frequency 5 GHz. For each propagating mode, fill in the following table. Waves are incident on the plates with an angle θ with respect to the normal to the plates. v_{pz} and v_g are the phase and group velocities respectively.

Mode	f_c (GHz)	θ (deg)	v_{pz} (m/s)	v_g (m/s)
TEM				
TE ₁				
TM ₁				
TE ₂				
TM ₂				

2. An air-filled rectangular waveguide has largest side $a = 1$ cm. Find the length of the side b , necessary to have identical cutoff frequency for the TE₂₀ and TM₁₁ modes.

3. An air-filled, X-band (8-12GHz), WC-94 circular waveguide has an inner diameter of 2.383 cm.

- Determine the cutoff frequencies of the TE₁₁, TM₀₁, and TE₂₁ modes.
- Find the modes that will propagate through this guide at 10 GHz.
- Find the frequency range within which only the TE₁₁ mode propagates.